

EE411 MATLAB Exercise-I

The Fourier series of the rectangular wave shown in Fig.1 is given by

$$g(t) = \frac{4}{\pi} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n} \sin(n\pi t)$$

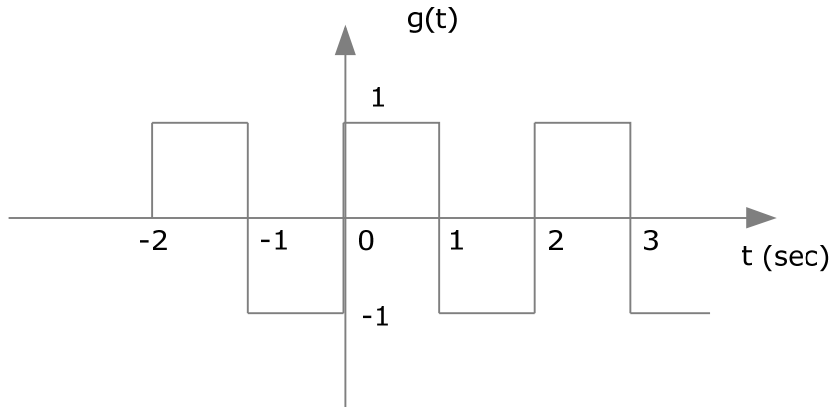


Fig. 1

(A) The signal $g(t)$ can be approximated by truncation of the Fourier series. Let

$$S_N(t) = \frac{4}{\pi} \sum_{n=1,3,5,\dots}^N \frac{1}{n} \sin(n\pi t), \quad (N \text{ is odd}), \text{ use MATLAB to plot}$$

- (1) the rectangular wave in Fig.1 and $S_1(t)$ in the same frame for comparison.
- (2) the rectangular wave in Fig.1 and $S_3(t)$ in the same frame for comparison.
- (3) the rectangular wave in Fig.1 and $S_5(t)$ in the same frame for comparison.
- (4) the rectangular wave in Fig.1 and $S_{11}(t)$ in the same frame for comparison.

Observe that $S_N(t)$ is approaching $g(t)$ as N increases.

(B) Find the power of the signal $g(t)$.

(C) If 90% power of the signal $g(t)$ is to be included in $S_N(t)$, what is the minimum value of N ?

(D) Plot $S_N(t)$, of which N is the minimum value required for $S_N(t)$ to include 90% of the total power of $g(t)$.