

## Using Geometry and Topology to Define Group Invariants

My goal is to define two (different but similar) invariants,  $\Sigma^1$  and  $\Omega^1$ , of infinite groups. Along the way, I will discuss some of the main characters involved such as: Cayley graphs, group actions, and the “sphere at infinity” of  $\mathbb{R}^m$ . Once these invariants have been defined, we will compute  $\Sigma^1$  and  $\Omega^1$  for some interesting groups. I will finish by discussing the relationship between  $\Sigma^1$  and  $\Omega^1$  and (time permitting) by discussing the higher dimensional analogs  $\Sigma^n$  and  $\Omega^n$ .